Creep behaviour of plane frame structures made of GFRP profiles

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1. Introduction

Glass Fiber Reinforced Polymer (GFRP) composite structural shapes manufactured by the pultrusion process have grown rapidly in the civil engineering industry in recent years [1]. These types of composite materials have been improved by progress in technology and started to be investigated from all perspectives [2]. GFRP profiles made from pultrusion process are frequently used as a design alternative where significant corrosion protection and chemical resistance is required [3]. Likewise, where accessibility is limited and lightweight structures are essential [4, 5] or where electromagnetic transparency is necessary, the pultruded GFRP profiles have come forward. Beside, their high strength to weight ratios, GFRP profiles can be used together with other construction materials accounting their benefits for improving the structural behaviour [6]. Since GFRP profiles can be produced in number of different section shapes similar to those used in the steel structures by several manufacturers around the world and can be cut to any desired length, it became an alternative material for the structural design [1]. However, beside these advantages, GFRP profiles are viscoelastic and show time-dependent behaviour. This issue is a disadvantage for the GFRP profiles which is required to be studied [1, 7].

In the literature, there are limited numbers of long-term tests for pultruded GFRP materials exist which is not sufficient to assess the creep behaviour of pultruded GFRP structures from different perspectives. Tests for time-dependent behaviour of GFRP profiles under static loads are often performed by coupon tests [8–10] and limited studies are performed on full-scale structures that are formed by pultruded GFRP profiles [11]. However, coupon tests are practical and cost-effective for investigating the time-dependent behaviour whereas full-scale tests provide more realistic results for determining the structural performance. In support of investigating time-dependent behaviour of structures that are formed with pultruded GFRP profiles, more studies are required to be performed for obtaining time-dependent strain redistributions within the cross-section of structural systems.

In this study, an analytical method is presented to investigate the creep behaviour of plane frame structures that are made of GFRP profiles under sustained loads and a full-scale test is performed using plane frame structure that is constructed using pultruded GFRP profiles and test results are compared with numerical analysis outcomes. In full-scale test frame, static load is applied from midpoint of the beam of the frame structure for 100 days and beam midpoint deflection and strains for particular points of the frame are monitored. Analytical results and test data are compared and satisfactory outcomes are observed.

2. Stress – strain – time relationship of viscoelastic structures

Stress – strain – time relationship for nonlinear viscoelastic material is accounted as below [12]:

\[ \sigma(t) = e_0 \left\{ B_0(e_0) + \sum_{i=1}^{n} B_i(e_i) g_i(t) \right\}, \]  (1)

where \( \sigma(t) \) is time-dependent stress function; \( B_i(e) \) is mechanical properties of the material related to deformation level; \( g_i(t) \) is time function selected to reflect the behaviour. \( B_i(e) \) and \( g_i(t) \) functions are shown as in Eq. (2) and Eq. (3), respectively.

\[ B_i(e) = k_0 |e|^{p_i-1}; \]  (2)

\[ g_i(t) = e^{-t/\lambda_i}; \]  (3)

where \( t \) is time, \( k_0, p_i \) and \( \lambda_i \) are material properties, \( e \) is strain. Similarly, for variable strain Eq. (1) is written as Eq. (4) [12]:

\[ \sigma(t) = \varepsilon(t) \left\{ B_0(\varepsilon(t)) + \sum_{i=1}^{n} B_i(\varepsilon(t)) \right\} - \sum_{i=1}^{n} \int_{0}^{t} \varepsilon(t) \frac{\partial}{\partial \tau} g_i(t-\tau) d\tau. \]  (4)

If \( g_i(t) \) is equal to unity and \( B_i(e) \) is accounted as constant for Eq. (4), then Hooke law as given in Eq. (5) can be obtained:

\[ \sigma(t) = \varepsilon(t) \left\{ B_0 + \sum_{i=1}^{n} B_i \right\} = E \varepsilon(t). \]  (5)

Likewise, if \( \beta_i \) is assumed as linear viscoelastic and the mechanical properties as deformation level \( B_i(e) = \beta_i = \text{constant}, \) \( \psi(0) = \beta_0 + \sum_{i=1}^{n} \beta_i \) and \( \psi(t) = \beta_0 + \sum_{i=1}^{n} \beta_i g_i(t) \) are written in Eq. (4), then Boltzmann superposition principle can be achieved as Eq. (6):

\[ \sigma(t) = \varepsilon(t) \psi(0) - \int_{0}^{t} \varepsilon(t) \sum_{i=1}^{n} \beta_i \frac{\partial}{\partial \tau} g_i(t-\tau) d\tau. \]  (6)
3. Application of moment-curvature relationship to a frame member

Stress and moment functions are derived by using strain and curvature relationship given in Eq. (7). Since stress – strain – time relation is given in Eq. (4), stress and moment functions are derived as in Eq. (8) and Eq. (9) as follows:

\[ \varepsilon(t) = -\frac{\varepsilon^2(t)}{\varepsilon x^2} = -z \Omega_x(t) ; \]  

\[ \sigma(t) = \left(-z \Omega_x(t)\right) \sum_{i=1}^{n} B_i \left(-z \Omega_x(t)\right) + \sum_{i=1}^{n} B_i \left(-z \Omega_x(t)\right) \sum_{i=1}^{n} \left[-z \Omega_x(t)\right] B_i \left(-z \Omega_x(t)\right) \frac{\varepsilon}{\varepsilon^2} g_i (t) \frac{d \varepsilon}{d \tau} \]  

\[ M = \int \left[ \left(-z \Omega_x(t)\right) \sum_{i=1}^{n} B_i \left(-z \Omega_x(t)\right) + \sum_{i=1}^{n} B_i \left(-z \Omega_x(t)\right) \sum_{i=1}^{n} \left[-z \Omega_x(t)\right] B_i \left(-z \Omega_x(t)\right) \frac{\varepsilon}{\varepsilon^2} g_i (t) \frac{d \varepsilon}{d \tau} \right] z \, dA , \]  

where \( \sigma(t) \) is time-dependent stress function, \( B_i \) is mechanical properties of the material related to deformation level, \( g_i(t) \) is time function selected to reflect the behaviour, \( \Omega_x(t) \) is time-dependent curvature function, \( z \) distance to the neutral axis.

If functions given with Eq. (2) are inserted into Eq. (9) and calculations steps are performed with writing Eq. (10) into the equations, moment – curvature relationship can be calculated using Eq. (11). In order to calculate curvature for a section from a moment value, Eq. (11) is written as in Eq. (12):

\[ I_m = 2b / (p_i + 2) (d/2)^{p_i+2} ; \]  

\[ M = -EI_x \Omega_x(t) + k_1 \Omega_x(t) [\Omega_x(t)]^{n-1} I_{pi} - \Omega_x(t) \sum_{i=1}^{n} k_i \Omega_x(t) [\Omega_x(t)]^{n-1} I_{pi} + \sum_{i=1}^{n} k_i e^{-i/\lambda_i} I_{pi} \int \Omega_x(t) \Omega_x(t) [\Omega_x(t)]^{n-1} e^{i/\lambda_i} d\tau ; \]  

\[ \Omega_x(t) = \frac{-M}{[EI_x - k_0 \Omega_x(t)]^{n-1} I_{pi} + \sum_{i=1}^{n} k_i \Omega_x(t) [\Omega_x(t)]^{n-1} I_{pi} - \frac{1}{\Omega_x(t)} \sum_{i=1}^{n} k_i e^{-i/\lambda_i} I_{pi} \int \Omega_x(t) \Omega_x(t) [\Omega_x(t)]^{n-1} e^{i/\lambda_i} d\tau} , \]  

where \( M \) bending moment; \( t \) time; \( k_i \) material coefficients; \( E \) modulus of elasticity; \( b \) width of section; \( d \) height of section; \( p_i \) material coefficient; \( I_0 \) moment of inertia of the section; \( I_{pi} \) is a value that is related with section properties and \( \Omega_x(t) \) is time-dependent curvature function.

Moment curvature relationship is calculated on the first step for the time-dependent analysis of viscoelastic frame system. Viscoelastic frame member with member length \( L_x \) is assumed and the moment value for any arbitrary section in \( 0 \leq x \leq L_x \) is known, then curvature is determined as in Eq. (12). In order to have more general form, Eq. (12) is written for different sections of \( x = 0, 1, 2, ..., k \) and curvature at any section of frame member for any time is defined by Eq. (13):

\[ \Omega_x^m (k \Delta x, r \Delta t) = -M (x,t) [EI_x - k_0 \Omega_x (k \Delta x, r \Delta t)]^{n-1} I_{pi} - \frac{1}{\Omega_x (k \Delta x, r \Delta t)} \sum_{i=1}^{n} k_i e^{-i/\lambda_i} I_{pi} \int [\Omega_x (k \Delta x, r \Delta t)]^{n-1} \Omega_x (k \Delta x, 0) e^{i/\lambda_i} + 2 \sum_{i=1}^{n} \Omega_x (k \Delta x, j \Delta t) [\Omega_x (k \Delta x, j \Delta t)]^{n-1} e^{i/\lambda_i} + \Omega_x^m (k \Delta x, r \Delta t) [\Omega_x^m (k \Delta x, r \Delta t)]^{n-1} e^{i/\lambda_i} , \]  

where \( m \) iteration number; \( k \) section number; \( r \) number of time interval; \( \Delta x \) and \( \Delta t \) change in location and time. In Eq. (13), curvature without a superscript \( \Omega \) means that it’s real value that is calculated before and remains same during the iteration. Similarly, if curvature with a superscript \( \Omega^m \) is the investigated curvature value and \( \Omega_x^m \) is the new curvature value after iteration.

Curvature value at any section at any time can be calculated using the moment values and Eq. (13). In order to calculate rotation values for a frame member as given in Fig. 1, moment value for an arbitrary section is determined by Eq. (14):

\[ M (x, t) = M_i (t) + M_s (t) + M_t (t) - \frac{M_i (t) + M_s (t)}{L_x} x , \]  

where \( M_i (t) \) and \( M_s (t) \) are end moment values for the time, \( L_x \) is length of frame member, \( x \) is location and \( t \) is time.

![Fig. 1 Frame member](image)

Virtual work is given as Eq. (15) and it is used for determination of end rotations for a member:

\[ 1 \times \phi_i (t) = \int_c \sigma \, dV , \]
where \( \phi_j(t) \) is time-dependent rotation at \( j \) end; \( \varepsilon \) strain; \( \sigma_v \) is stress for virtual system; \( V \) is volume.

Eq. (7), Eq. (8) and Eq. (12) are put into Eq. (15) and consequently Eq. (16) is obtained. Integral that is in Eq. (16) is similar with Eq. (11) and this is accounted as

\[
1 \times \phi_j(t) = \int_{0}^{l_j} \Omega_j(x,t) \left[ \sum_{i=1}^{n} k_i \left( \int_{0}^{z} \Omega_i(x,t) \left[ \left( E - k_0 \right) \Omega_i(x,t) \right]^{n-1} - \int_{0}^{r_e} e^{\tau_0} \right) dA \right] dx;
\]

\[
1 \times \phi_j(t) = \int_{0}^{l_j} \Omega_j(x,t) m_j(x) dx; \tag{17}
\]

\[
\phi_j(t) = \int_{0}^{l_j} \left( 1 - \frac{x}{L_j} \right) \Omega_j(x,t) dx; \tag{18}
\]

\[
\phi_k(t) = \int_{0}^{l_k} \frac{x}{L_k} \Omega_k(x,t) dx, \tag{19}
\]

where \( \Omega_j(x,t) \) location and time-dependent curvature; \( \phi_j(t) \) and \( \phi_k(t) \) are time-dependent end rotations for \( j \) and \( k \) ends of frame member; \( L_j \) length of the member; \( E \) modulus of elasticity; \( x \) location; \( t \) time; \( z \) distance to neutral axis; \( k_i, p_i \) and \( \dot{\lambda} \) material coefficients.

If the end moments of a frame member and loads acting on the frame member are known, curvature is calculated by Eq. (13). Consequently, curvature results are used in Eqs. (18) and (19) in order to calculate end rotations of the frame member. Viscoelastic member is given in form of equivalent linear elastic member and rigidity coefficients of the equivalent linear member are given in Eqs. (20) and (21). In these equations also, member section is accounted constant in the length of the member and in order to have the equation in more general form \( \Delta \) displacement term is added.

\[
M_j = s_1 \left( \theta_j(t) - \frac{\Delta}{L_j} \right) + s_2 \left( \theta_k(t) - \frac{\Delta}{L_k} \right); \tag{20}
\]

\[
M_k = s_2 \left( \theta_j(t) - \frac{\Delta}{L_j} \right) + s_1 \left( \theta_k(t) - \frac{\Delta}{L_k} \right), \tag{21}
\]

where \( M_j \) and \( M_k \) are moment values for the \( j \) and \( k \) ends of the member; \( \Delta \) is displacement between frame ends; \( L_i \) is the length of the member; \( \theta_j(t) \) and \( \theta_k(t) \) are time-dependent rotations for the \( j \) and \( k \) ends of the member; \( s_1 \) and \( s_2 \) are rigidity coefficients of member. These rigidity coefficients are dependent to moment values and are calculated for frame members. The viscoelastic deformation approach is applied for analysis. \( M_j \) value, which is calculated at the end of calculation, should be equal to the moment value that is accepted to be known prior to the calculation process. However, in the beginning of the calculation, since moment value is not known in advance, a trial \( M_j \) value is accepted. For a trial value, linear elastic analysis results can be used. Moment value \( M_j \) that is calculated at the end of the calculation, is not equal to \( M_j \) accounting a tolerance value, same process is performed accounting \( M_i \) as \( M_j \) value and this process is repeated up to the calculated moment value is equal to \( M_j \) in adequate tolerance. This process is repeated for \( t = 0, \Delta t, 2\Delta t, \ldots, r\Delta t \) and time-dependent changes in internal forces and joint displacements of viscoelastic frame system is calculated.

In order to investigate time-dependent behaviour of plane frame structures a computer program is developed using the procedure described in this section. A GFRP frame is modelled and analysed under sustained loads for the time period of 100 days.

4. Time-dependent tests under sustained loads

A plane frame that is formed with GFRP profiles is tested for 100 days under sustained loads. Static load is applied from the midpoint of the beam of the frame and strain, displacement values for some selected points are monitored during the test. Likewise, three point beam bending test is performed in order to evaluate the behavior and results of this test is used for determination of material coefficients for the analytical function. In order to perform creep tests and eliminate possible geometric influences on the structural behavior, GFRP profiles are supplied from same stock having same material and section properties [13]. Since, it is important to keep stress level same for determining creep behavior [14], static loads are used instead of hydraulic loading systems to keep the stress level constant during the test period. Time independent mechanical properties of the GFRP profiles are also determined using three point bending test described in ASTM standard [15]. Elasticity modulus is 21058 MPa, shear modulus is 855 MPa, and flexural strength is 464 MPa for coupons that are taken from GFRP profiles.

Three point bending test of GFRP beam with 40 mm × 40 mm × 4 mm box section under sustained load is performed at first as shown in Fig. 2. Beam clear length is 3200 mm and load is applied from the midpoint of the beam and section stress is 23.2 MPa.

![Three point bending test model for GFRP box beam](image)

Midpoint deflection is monitored by using LVDT and strain value is monitored by strain gauges for time-dependent three point bending test for 30 days in Fig. 3.
A plane frame made of GFRP profiles is used for testing the time-dependent behaviour for 100 days under sustained loads. Static load is applied from the midpoint of the beam member of the plane frame and structural behaviour is monitored during the test with the relevant time intervals. Column and beam members are formed with 40 mm × 40 mm × 4 mm box GFRP sections as given in Fig. 4. Beam length and column height is 1800 mm. Beam to column connection is made with top-and-seat angles with L 100 mm × 10 mm GFRP section and steel M12 (8.8) bolts are used as shown in Fig. 5. Since connection is formed with relatively high angle sections than beam member as presented in Fig. 6 and relatively low load level is used in the test, the connection behaviour is assumed as rigid. Moreover, a strain-gauge is used at theoretical moment zero location in the test frame and the strain value is controlled for validating rigid connection assumption.

Midpoint deflection of the beam of the frame and strain of four locations on the frame are monitored using LVDT and stain-gauges as given in Fig. 4. Since, it is a characteristic point, midpoint deflection is reported. Besides, strain values are monitored for station points; S_1 at the midpoint of the beam member of the frame, S_2 and S_3 on the column at 300 mm below the beam-column connection and 300 mm above the base plate. Also, S_4 is placed at theoretical zero strain point on the beam.

Applied load level is selected accounting the serviceability limits of ASCE as L/180 where L is the length of the beam [16]. After loading is performed, the vertical deflection of midpoint of the beam is 10.34 mm. The stress value for this load level is calculated as 21.6 MPa which is approximately 5% of the beam bending capacity. This value is lower than the 20% limit which is suggested for GFRP systems in many studies [1].

This load is kept for 100 days and data is recorded for the time intervals as 10 seconds for the first hour, and hourly readings for remaining 23 hours and daily for following 99 days.

5. Evaluation of test results with analytical approach

Test results are evaluated using stress – strain – time relationship derived in the analytical part of the study. Material coefficients are determined from time-dependent three point beam bending test and these coefficients are used in analytical solving of one bay frame numerically. Test results of one bay frame are compared with the analytical study results and outcomes are discussed.

In order to determine material coefficients for the analytical approach, three point beam bending test results are used. GFRP beam’s midpoint strain and time relation is plotted and nonlinear least-squares method is used for curve fitting as in Fig. 7. Material coefficients are determined as k_0 = 3482, k_1 = 3505, p_0 = 1.086, p_1 = 1.101, λ_1 = 11.75.
Test results and analytical calculations for time-dependent behaviour of one bay frame are compared. Vertical deflection of beam midpoint – time graphic is given in Fig. 8, strain – time graphics for selected points on the GFRP frame are presented in Figs. 9-11. Also, analytical calculation results are given for bending moment – time graphics for the selected points in Figs. 12-14.

Increase in the vertical displacement of the midpoint of the frame’s beam for 100 days is given in Fig. 8 and determined as 11.5% and 11.6% from test and analytical results. Strain of the midpoint of the frame’s beam is also monitored and results are presented in Fig. 9. These results show that strain increase for the test period of 100 days for the midpoint of the frame’s beam are 12.9% and 12.8% for test data and analytical results.

Bending moment values are calculated using analytical method for the same sections that strain values are monitored. Bending moment – time relationship for beam midpoint, the column sections at 300 mm below the beam-column connection and 300 mm above the base plate are presented using analytical calculation results in Figs. 12-14.

Results show that bending moment value for the midpoint of the beam of the frame decreases with time under sustained loading. However, bending moment of the column sections, which are for 300 mm lower from beam-to-column connection and 300 mm over the base plate of the column, increases. These results show that time-dependent behaviour of GFRP profiles are affecting the structural behaviour of frames. These values present the moment redistribution in viscoelastic member sections of the GFRP frame under long term loads.

6. Conclusions

Time-dependent behaviour of GFRP profiles under sustained loads is investigated using both analytical approach and test data. A plane frame made of GFRP profiles is tested under sustained loads and strain, deflections are monitored. Also, an analytical method is presented for
calculation of strain and deflections for the GFRP frame. Results of the analytical calculation and test data are evaluated and the following conclusions are drawn:

1. Structures that are formed with GFRP profiles are viscoelastic and vertical midpoint deflection are increased 11.5% for 100 days for the current test. The increase is in lowering trend and this shows the nature of viscoelastic behaviour under sustained loads. Likewise, strain values are monitored from different locations on the frame members and strain values are in the trend of an increase. Strain values, where the vertical displacement is monitored, show an increase of 12.9% for 100 days at the end of the test.

2. Analytical calculation results show good compliance with full-scale test data in displacement values and also in strain data. The difference between analytical results and test data are not more than 1% for all compared station points.

3. Since all the sections on a frame cannot be reported from full-scale tests, analytical calculation give engineers an opportunity to foresee the time-dependent values of displacement and strain for any desired location on the frame. Furthermore, bending moment values can be determined by analytical calculation and structural design can be performed accounting possible time-dependent effects for GFRP frame structures.

4. Bending moment values for GFRP frame member sections, increase or decrease due to time regarding the loading of the frame. However, changes in bending moment values are not more than 1% for all sections at particular locations of the frame.

5. Since, coupon tests are generally focused in the literature, this study contributes to full-scale tests of the time-dependent behaviour of frame structures formed using GFRP profiles from both analytical and experimental perspective.

References


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CREEP BEHAVIOUR OF PLANE FRAME STRUCTURES MADE OF GFRP PROFILES

Summary

A methodology is presented for analytical calculation of creep behavior of plane frames made of glass fiber reinforced polymer (GFRP) profiles and an experimental study is carried out in order to evaluate the analytical calculation results. In order to account nonlinear viscoelastic material behavior, stress – strain – time relationship of plane frame is given and creep behavior of plane frame structure is investigated. Material coefficients for the creep functions are determined using three point beam bending test results. In order to validate the analytical approach, a plane frame made of GFRP profiles is tested under sustained loads for 100 days and displacements, strains are monitored. Strain and displacement values that are calculated using analytical method show good agreement with the full-scale test data.

Keywords: viscoelastic behaviour, creep, glass fiber reinforced polymer profiles, GFRP frame.