# Multiscale Analysis and Numerical Simulation of Hydrodynamic Inclined Fixed Pad Thrust Slider Bearing with Ultra Low Surface Separation Involving Surface Roughness

# Weiwei ZHU, Chen HUANG, Chao WANG, Yongbin ZHANG

College of Mechanical Engineering, Changzhou University, Changzhou, Jiangsu Province, China, E-mails: yongbinzhang@cczu.edu.cn; engmech1@sina.com (Corresponding author) crossref http://dx.doi.org/10.5755/j02.mech.30821

# 1. Introduction

The development of modern industry has put forward higher requirements for the lubrication performance of hydrodynamic slider bearings. In fact, the manufactured bearing surface often has somewhat surface roughness. When the bearing surface roughness is comparable to the bearing clearance, the surface roughness should influence the bearing performance [1-3].

There have been a lot of studies on mixed lubrication by considering the surface roughness effect. It was ever popularly followed that in a hydrodynamic lubricated contact the load is carried by both the hydrodynamic film and the solid asperity contact [4-6]. There have been the arguments that such a model may be over simplified because of neglecting the effect of the physically adsorbed layer on the lubricated surface.

Molecular dynamics simulations (MDS) as well as experiments showed the existence of the physically adsorbed boundary layer in a hydrodynamic contact [7-10]. However, there were the difficulties in simulating the behavior of the adsorbed layer in an engineering hydrodynamic problem because of MDS taking over large cost of computer storage and computational time. In recent years, Zhang developed the closed-form explicit flow equations respectively for the adsorbed layer flow and the intermediate continuum fluid flow in the two-dimensional multiscale flow problem [11]. The advantage of this multiscale approach is to give fast solution and be able to solve the engineering problem.

The present paper attempts to study the effect of the surface roughness in the hydrodynamic inclined fixed pad thrust slider bearing with ultra low surface separations considering the physically adsorbed boundary layer. It is aimed to give the new results of the surface roughness influence on this mode of bearing.

## 2. Studied bearing

Fig. 1 shows the hydrodynamic inclined fixed pad thrust slider bearing with ultra low surface separation involving surface roughness. This bearing occurs when the load is very heavy and the bearing surface is not smooth so that there is only a very small gap between the bearing surfaces.

The upper surface of the bearing is stationary with the sinusoidal roughness, and the lower surface is assumed as perfectly smooth and moves with the speed u. The whole width of the bearing is l, and the tilting angle of the bearing is  $\theta$ . The upper and lower surfaces are assumed as identical, and the adsorbed layers on both of them have the same thickness  $h_{bf}$ . The intermediate continuum fluid film thickness is h, the surface separation is  $h_{tot}$ , and that on the exit of the bearing is  $h_{tot,o}$ . The used coordinates are also shown in Fig. 1.



Fig. 1 Hydrodynamic inclined fixed pad thrust slider bearing with ultra low clearance involving surface roughness

# 3. Numerical analysis

Considering that the viscosity and density of the fluid will be affected by the pressure in this severe condition, the piezo-viscous effect of the fluid is considered in the present study. In addition to this, this study is based on the following assumptions: a) the side leakage is negligible; b) no interface slippage occurs on any interface; c) the flow is isothermal; d) the working condition is steady-state.

## 3.1. For the present bearing

According to the nanoscale flow equation [12], the total mass flow rate per unit contact length through the boundary lubrication area (without the intermediate continuum fluid film) is:

$$q_{m} = \frac{dp}{dx} \frac{S \rho_{bf,2}^{eff} h_{tot}^{3}}{12\eta_{bf,2}^{eff}} - \frac{u}{2} h_{tot} \rho_{bf,2}^{eff}, \qquad (1)$$

where:  $h_{tot} = h_{tot,o} + xtan\theta + R_z sin(\omega x + \varphi)/2$ ; *p* is the film pressure;  $\rho_{bf,2}^{eff}$  and  $\eta_{bf,2}^{eff}$  are respectively the average density and the effective viscosity of the adsorbed layer in the boundary lubrication area; *S* is the parameter accounting for the non-continuum effect of the adsorbed layer.

According to the multiscale flow equation [11], the total mass flow rate per unit contact length through the sandwich film lubrication area (with the intermediate continuum fluid film) is:

$$q_{m} = \frac{\rho_{bf,1}^{eff}h_{bf}^{3}}{\eta_{bf,1}^{eff}}\frac{dp}{dx} \left[ \frac{F_{1}}{6} - \left( 1 + \frac{1}{2\lambda_{bf}} - \frac{q_{0} - q_{0}^{n}}{q_{0}^{n-1} - q_{0}^{n}}\frac{\Delta_{n-2}}{h_{bf}} \right) \frac{\varepsilon}{1 + \frac{\Delta x}{D}} \right] + \frac{\rho h^{3}}{\eta_{bf,1}^{eff}}\frac{dp}{dx} \left[ \frac{F_{2}\lambda_{bf}^{2}}{6} - \frac{\lambda_{bf}}{1 + \frac{\Delta x}{D}} \left( \frac{1}{2} + \lambda_{bf} - \frac{q_{0} - q_{0}^{n}}{q_{0}^{n-1} - q_{0}^{n}}\frac{\Delta_{n-2}\lambda_{bf}}{h_{bf}} \right) \right] - uh_{bf}\rho_{bf,1}^{eff} - \frac{\rho h^{3}}{12n}\frac{dp}{dx} - \frac{\rho uh}{2},$$

$$(2)$$

where:  $\lambda_{bf} = h_{bf}/h$ , *n* is the equivalent number of the fluid molecules across the adsorbed layer thickness; *D* and  $\Delta x$ are respectively the fluid molecule diameter and the separation between the neighboring fluid molecules in the adsorbed layer in the *x* coordinate direction;  $\Delta_{n-2}$  is the separation between the neighboring fluid molecules across the adsorbed layer thickness just on the boundary between the adsorbed layer and the intermediate continuum fluid;  $\rho$  and  $\eta$  are respectively the bulk density and the bulk viscosity of the fluid; pressure;  $\rho_{bf,2}^{eff}$  and  $\eta_{bf,2}^{eff}$  are respectively the average density and the effective viscosity of the adsorbed layer in the sandwich film flow;  $q_0 = \Delta_{j+1} / \Delta_j$ ;  $q_0$  is averagely constant;  $\Delta_j$  is the separation between the  $(j + 1)^{th}$  and  $j^{th}$  fluid molecules across the adsorbed layer thickness;

$$\begin{split} F_{1} &= \eta_{bf,1}^{eff} \left( 12D^{2}\Psi + 6D\Phi \right) / h_{bf}^{3}, \\ F_{2} &= 6\eta_{bf,1}^{eff} D \left( n-1 \right) \left( l \varDelta_{l-1} / \eta_{line,l-1} \right)_{avr,n-1} / h_{bf}^{2}, \\ \varepsilon &= (2DI + II) / \left[ h_{bf} \left( n-1 \right) \left( \varDelta_{l} / \eta_{line,l} \right)_{avr,n-1} \right], \text{ here} \\ I &= \sum_{i=1}^{n-1} i \left( \varDelta_{l} / \eta_{line,l} \right)_{avr,i}, \ \Psi &= \sum_{i=1}^{n-1} i \left( l \varDelta_{l-1} / \eta_{line,l-1} \right)_{avr,i}, \\ II &= \sum_{i=0}^{n-2} \left[ i (\varDelta_{l} / \eta_{line,l})_{avr,i} + (i+1) (\varDelta_{l} / \eta_{line,l})_{avr,i+1} \right] \varDelta_{l}, \\ \Phi &= \sum_{i=0}^{n-2} \left[ i \left( l \varDelta_{l-1} / \eta_{line,l-1} \right)_{avr,i} + (i+1) \left( l \varDelta_{l-1} / \eta_{line,l-1} \right)_{avr,i+1} \right] \varDelta_{i}, \\ i \left( \varDelta_{l} / \eta_{line,l-1} \right)_{avr,i} &= \sum_{j=1}^{i} \varDelta_{j-1} / \eta_{line,j-1}, \\ i \left( l \varDelta_{l-1} / \eta_{line,l-1} \right)_{avr,i} = \sum_{j=1}^{i} j \varDelta_{j-1} / \eta_{line,j-1}; \quad \eta_{line,j-1} \text{ is the} \end{split}$$

local viscosity between the  $j^{th}$  and  $(j-1)^{th}$  and fluid molecules across the adsorbed layer thickness, and

$$\eta_{line,j} / \eta_{line,j+1} = q_0' \; .$$

The fluid bulk viscosity is expressed as:  $\eta = \eta_a exp\left\{ (ln\eta_a + 9.67) \left[ (1+5.1 \times 10^{-9} p)^G - 1 \right] \right\},$  where  $G = \alpha / \left[ 5.1 \times 10^{-9} (ln\eta_a + 9.67) \right]$  and  $\eta_a$  is the fluid bulk viscosity at atmospheric pressure. The fluid bulk density is expressed as:  $\rho = \rho_a (1+\beta \cdot p)$ , where  $\rho_a$  is the fluid bulk density at atmospheric pressure and  $\beta$  is constant.

As shown in Fig. 1, there are the (N+1) discretized points evenly distributed in the whole area. According to Eq. (1), the pressure gradient on the  $K_{th}$  discretized point is:

$$\frac{dp}{dx}\Big|_{K} = \frac{p_{K} - p_{K-1}}{\delta_{x}} = \frac{12\eta_{bf,2}^{eff}\left(q_{m} + \frac{u}{2}h_{tot,K}\rho_{bf,2}^{eff}\right)}{S\rho_{bf,2}^{eff}h_{tot,K}^{3}}$$

for 
$$h_{tot,K} \le 2h_{bf}$$
. (3)

According to Eq. (2), the pressure gradient on the  $K^{th}$  discretized point is:

$$\frac{dp}{dx}\Big|_{\kappa} = \frac{p_{\kappa} - p_{\kappa-1}}{\delta_{x}} = \frac{a(h_{tot,\kappa} - 2h_{bf}) + b}{\left[c(h_{tot,\kappa} - 2h_{bf})^{3} + d\right]cot\theta},$$
  
for  $h_{tot,\kappa} \le 2h_{bf}$ . (4)

where:  $h_{tot,K}=h_{tot,o}+x_Ktan\theta+R_zsin(\omega x_K+\varphi)/2$ ; a = up/2,  $b = q_m + uh_{bf}\rho_{bf,1}^{eff}$ ,

$$c = \frac{F_2 \lambda_{bf}^2 \rho tan\theta}{6\eta_{bf,1}^{eff}} - \frac{\rho tan\theta}{12\eta} - \frac{\lambda_{bf} \rho tan\theta}{\eta_{bf,1}^{eff} \left(1 + \frac{\Delta x}{D}\right)} \left(\frac{1}{2} + \lambda_{bf} - \frac{q_0 - q_0^n}{q_0^{n-1} - q_0^n} \frac{\Delta_{n-2} \lambda_{bf}}{h_{bf}}\right), \quad (5)$$

$$d = \frac{n_{bf} \rho_{bf,1}^{eff}}{6\eta_{bf,1}^{eff}} - \frac{h_{bf}^3 \rho_{bf,1}^{eff} tan\theta}{\eta_{bf,1}^{eff}} \left(1 + \frac{1}{2\lambda_{bf}} - \frac{q_0 - q_0^n}{q_0^{n-1} - q_0^n} \frac{\Delta_{n-2}}{h_{bf}}\right) \frac{\varepsilon}{1 + \frac{\Delta x}{D}}.$$
 (6)

The backward difference gives that:

$$p_{K} - p_{K-1} = \frac{dp}{dx} \Big|_{K} \cdot \delta_{x}, \tag{7}$$

where:  $P_K$  and  $P_{K-1}$  are respectively the hydrodynamic pressures on the  $K^{th}$  and  $(K-1)^{th}$  discretized points and  $\delta_x = l/N$ .

Since  $p_0 = 0$ , it is easily written that  $p_K = \sum_{M=1}^{K} (p_M - p_{M-1})$ , where:

$$p_{M} - p_{M-1} = \frac{12\eta_{bf,2}^{eff} \left(q_{m} + \frac{u}{2}h_{tot,M}\rho_{bf,2}^{eff}\right)}{S\rho_{bf,2}^{eff}h_{tot,M}^{3}}\delta_{x},$$
  
for  $h_{tot,M} \le 2h_{bf},$  (8)

$$p_{M} - p_{M-1} = \frac{a(h_{tot,M} - 2h_{bf}) + b}{\left[c(h_{tot,M} - 2h_{bf})^{3} + d\right]\cot\theta}\delta_{x},$$
  
for  $h_{tot,M} > 2h_{bf}.$  (9)

The load per unit contact length carried by the bearing is then calculated as:

$$w = \delta_x \sum_{K=1}^N p_K.$$
 (10)

3.2. For the classical mode of the bearing

For comparison, the numerical analysis of the classical mode of the bearing (ignoring the adsorbed layer) is carried out in this section.



Fig. 2 The classical mode of the bearing with surface roughness

As shown in Fig. 2, for the classical mode of the bearing, there are the (N+1) discretized points evenly distributed in the whole area. The pressure gradient on the  $C^{th}$ discretized point is:

$$\frac{dp}{dx}\Big|_{C} = -\frac{6u\eta}{h_{tot,C}^{2}} - \frac{12\eta q_{m,C}}{\rho h_{tot,C}^{3}},\tag{11}$$

where:  $h_{tot,C} = h_{tot,o} + x_C tan\theta + R_z sin(\omega x_C + \varphi)/2$  and  $q_{m,C}$  is the mass flow rate per unit contact length in the classical mode of bearing.

The finite difference gives that  $dp/dx|_{c} = (p_{c} - p_{c-1})/\delta_{x}$ ,  $p_{c}$  and  $p_{c-1}$  are respectively the hydrodynamic pressures on the  $C^{th}$  and  $(C-1)^{th}$  discretized points. Since  $p_0=0$ , it is easily written that  $p_C = \sum_{j=1}^{C} (p_j - p_{j-1})$ . The pressure on the  $C^{th}$  discretized

point is then:

$$p_{C} = -6\delta_{x} \sum_{j=1}^{C} \left( \frac{u\eta}{h_{tot,j}^{2}} + \frac{2\eta q_{m,C}}{\rho h_{tot,j}^{3}} \right),$$
  
for  $C = 1, 2, ..., N.$  (12)

The load per unit contact length carried by the bearing is calculated as:

$$w = \delta_x \sum_{C=1}^{N} p_C.$$
<sup>(13)</sup>

# 3.3. Normalization

The dimensionless parameters are defined as fol-

lows: 
$$\overline{\delta}_x = \frac{\overline{\delta}_x}{h_{bf}}, \ \overline{\delta}_{x,C} = \frac{\overline{\delta}_x}{h_{tot,o}}, \ H_{tot,M} = \frac{h_{tot,M}}{h_{bf}},$$
  
 $H_1 = \frac{h_{bf}}{h_{cr,bf,1}}, \ H_2 = \frac{h_{tot}}{h_{cr,bf,2}}, \ M_1 = \frac{\eta}{\eta_a}, \ N_1 = \frac{\rho}{\rho_a}, \ \overline{c} = \frac{c\eta_a}{\rho_a},$   
 $\overline{d} = \frac{d\eta_a}{\rho_a h_{bf}^3}, \ Cy_1 = \frac{\eta_{bf,1}^{eff}}{\eta}, \ Cy_2 = \frac{\eta_{bf,2}^{eff}}{\eta}, \ Cq_1 = \frac{\rho_{bf,1}^{eff}}{\rho},$   
 $Cq_2 = \frac{\rho_{bf,2}^{eff}}{\rho}, \ Q_m = \frac{q_m}{u\rho_a h_{tot,o}}, \ P = \frac{ph_{tot,o}}{u\eta_a}, \ W = \frac{w}{u\eta_a}.$ 

Here  $h_{cr,bf,1}$  is the critical thickness for characterizing the rheological properties of the adsorbed layer in the sandwich flow, and  $h_{cr,bf,2}$  is the critical thickness for characterizing the rheological properties of the adsorbed layer in the boundary lubrication area.

## 3.3.1. For the present bearing

The dimensionless pressure on the  $K^{th}$  discretized point is:  $P_K = \sum_{M=1}^{K} (P_M - P_{M-1})$ , where:

$$P_{M} - P_{M-1} = \overline{\delta}_{x} \left( \frac{12Cy_{2}M_{1}Q_{m}H_{tot,o}^{2}}{SCq_{2}N_{1}H_{tot,M}^{3}} + \frac{6Cy_{2}M_{1}H_{tot,o}}{SH_{tot,M}^{2}} \right),$$
  
for  $H_{tot,M} \leq 2,$  (14)

$$\begin{split} P_{M} - P_{M-1} &= \\ &= \overline{\delta}_{x} \frac{\left(H_{tot,M} - 2\right) H_{tot,o} N_{1} / 2 + Cq_{1} H_{tot,o} N_{1} + Q_{m} H_{tot,o}^{2}}{\left[\overline{c} \left(H_{tot,M} - 2\right)^{3} + \overline{d}\right] Cot\theta}, \end{split}$$

for 
$$H_{tot,M} > 2$$
, (15)

where:  $Q_m$  is the dimensionless mass flow rate per unit contact length through the bearing:

$$\overline{c} = \frac{N_1 F_2 \lambda_{bf}^2 tan\theta}{6C y_1 M_1} - \frac{N_1 tan\theta}{12M_1} - \frac{\lambda_{bf} N_1 tan\theta}{C y_1 M_1 \left(1 + \frac{\Delta x}{D}\right)} \left(\frac{1}{2} + \lambda_{bf} - \frac{q_0 - q_0^n}{q_0^{n-1} - q_0^n} \frac{\Delta_{n-2} \lambda_{bf}}{h_{bf}}\right), \quad (16)$$

$$\overline{d} = \frac{Cq_1 N_1 F_1 tan\theta}{6Cy_1 M_1} - \frac{Cq_1 N_1 tan\theta}{Cy_1 M_1} \left( 1 + \frac{1}{2\lambda_{bf}} - \frac{q_0 - q_0^n}{q_0^{n-1} - q_0^n} \frac{\Delta_{n-2}}{h_{bf}} \right) \frac{\varepsilon}{1 + \frac{\Delta x}{D}}, \quad (17)$$

The dimensionless load carried by the bearing is:

$$W = \overline{\delta}_x \sum_{K=1}^{N-1} P_K.$$
 (18)

## 3.3.2. For the classical mode of bearing

The dimensionless pressure on the  $C^{th}$  discretized point is:

$$P_{C} = -6\overline{\delta}_{x,C} \sum_{j=1}^{C} \left( \frac{M_{1}}{H_{tot,j}^{2}} + \frac{2M_{1}Q_{m,C}}{N_{1}H_{tot,j}^{3}} \right),$$
  
for  $C = 1, 2, ..., N.$  (19)

where:  $Q_{m,c}$  is the dimensionless mass flow rate per unit contact length through this bearing.

The dimensionless load carried by the bearing is:

$$W = \overline{\delta}_{x,C} \sum_{C=1}^{N-1} P_C.$$
<sup>(20)</sup>

#### 3.4. Numerical solution procedure

Fig. 2 shows the numerical solution procedure, from which it can be seen that the calculation results are converged by controlling the precision of  $Q_m$ . Then, substitute  $Q_m$  into Eqs. (14) or (15) to calculate the pressure on each discrete point, and get the final result for the present bearing. For the classical bearing, the numerical calculation method is the same.



Fig. 3 The numerical solution procedure

# 4. Calculation

Exemplary calculations were carried out for the

following input parameter values:

 $D = 0.5 \text{ nm}; \Delta_{n-2}/D = \Delta_x/D = 0.15; l = 100 \text{ µm}; \theta = 1.0 \times 10^{-4} \text{ rad}; \alpha = 1.6 \times 10^{-8} \text{ m}^2/\text{N}; \beta = 0.4 \times 10^{-9} \text{ Pa}^{-1}; u = 1 \times 10^{-6} \text{ m/s}; w = 2\pi/\lambda; \lambda = l/20; \varphi = \pi; \eta_a = 0.03 \text{ Pa} \cdot \text{s}.$ 

The parameters  $Cq_1(H_1)$  and  $Cq_2(H_2)$  are generally expressed by the following well used formula:

$$Cq(H) = \begin{cases} 1 & , \text{ for } H \ge 1 \\ m_0 + m_1 H + m_2 H^2 + m_3 H^3 & , \text{ for } 0 < H < 1 \end{cases}$$
 (21)

where: *H* is  $H_1$  or  $H_2$ ;  $m_0$ ,  $m_1$ ,  $m_2$  and  $m_3$  are respectively shown in Table 1.

The parameters  $Cy_1(H_1)$  and  $Cy_2(H_2)$  are generally expressed by the following well used formula:

$$Cy(H) = \begin{cases} 1 & , \text{ for } H \ge 1 \\ a_0 + \frac{a_1}{H} + \frac{a_2}{H^2} & , \text{ for } 0 < H < 1 \end{cases}$$
 (22)

where: *H* is  $H_1$  or  $H_2$ ;  $a_0$ ,  $a_1$  and  $a_2$  are respectively shown in Table 2.

The parameter  $S(H_2)$  is expressed by the following well used formula:

$$S(H_2) = \begin{cases} -1 & , \text{ for } H_2 \ge 1 \\ \left[ n_0 + n_1 \left( H_2 - n_3 \right)^{n_2} \right]^{-1} & , \text{ for } n_3 < H_2 < 1 \end{cases}$$
(23)

where:  $n_0$ ,  $n_1$ ,  $n_2$  and  $n_3$  are respectively shown in Table 3.

The parameters  $F_1$ ,  $F_2$  and  $\varepsilon$  are respectively formulated as [11]:

$$F_1 = 0.18 \left(\frac{\Delta_{n-2}}{D} - 1.905\right) (lnn - 7.897), \tag{24}$$

$$F_{2} = (-3.707E - 4) \left( \frac{\Delta_{n-2}}{D} - 1.99 \right) (n + 64) \cdot \left( q_{0} + 0.19 \right) (\gamma + 42.43),$$
(25)

$$\varepsilon = (4.56E - 6) \left( \frac{\Delta_{n-2}}{D} + 31.419 \right) (n + 133.8) \cdot (q_0 + 0.188) (\gamma + 41.62),$$
(26)

The weak, medium and strong fluid-bearing surface interactions were respectively used. They respectively have the operational parameter values shown in Tables 1-4. Table 1

Popularly used fluid density data for different fluid-bearing surface interactions

Parameter Interaction	$m_0$	$m_1$	<i>m</i> <sub>2</sub>	<i>m</i> 3
Strong	1.43	-1.723	2.641	-1.347
Medium	1.30	-1.065	1.336	-0.571
Weak	1.116	-0.328	0.253	-0.041

Popularly used fluid viscosity data for different fluid-bearing surface interactions

Parameter Interaction	$a_0$	<i>a</i> 1	<i>a</i> 2
Strong	1.8335	-1.4252	0.5917
Medium	1.0822	-0.1758	0.0936
Weak	0.9507	0.0492	1.6447E-4

Table 3

Popularly used fluid non-continuum property data for different fluid-bearing surface interactions

Parameter Interaction	$n_0$	$n_1$	$n_2$	<i>n</i> <sub>3</sub>
Strong	0.4	-1.374	-0.534	0.035
Medium	-0.649	-0.343	-0.665	0.035
Weak	-0.1	-0.892	-0.084	0.1

Popularly used values of n,  $q_0$ ,  $\gamma$ ,  $h_{cr,bf,1}$  and  $h_{cr,bf,2}$  for different fluid-bearing surface interactions

Parameter Interaction	п	$q_0$	γ	$h_{cr,bf,1}$ , nm	$h_{cr,bf,2}$ , nm
Strong	8	1.2	1.5	40	80
Medium	5	1.1	1	20	40
Weak	3	1.03	0.5	7	14

#### 5. Results

For the weak fluid-bearing surface interaction, in the bearing with  $R_z > 13.4$  nm will occur the coexistence of the boundary lubrication and the sandwich film lubrication when  $h_{tot,o} = 10$  nm. For  $R_z < 13.4$  nm is only present the sandwich film lubrication. For medium and strong fluid-bearing surface interactions, the cases are similar respectively for  $R_z > 8.96$  nm and  $R_z > 2.72$  nm.



fluid-bearing surface interactions ( $R_z = 14 \text{ nm}$ )

Fig. 4 Dimensionless pressure distributions in the bearing for different surface roughness  $R_z$  and different fluid-bearing surface interactions when  $h_{tot,o} = 10$  nm and  $\theta = 1 \times 10^{-4}$  rad

## 5.1. Pressure distribution

Figs. 4, a-d plot the dimensionless pressure distributions in the bearing for different fluid-bearing surface interactions when the piezo-viscous effect is considered.

As shown in Figs. 4, a-c, the hydrodynamic pressure for the rough surface is always greater than that for the smooth surface, and the hydrodynamic pressure increases significantly with the increase of the surface roughness.

Fig. 4, d shows the pressure distributions in the bearing for different fluid-bearing surface interactions when  $h_{tot,o} = 10$  nm and  $R_z < 14$  nm. The results show that

the hydrodynamic pressure for the weak interaction is less different from that calculated from classical hydrodynamic lubrication theory, while for the medium and strong interactions they are more different from the classical calculations. The pressure for the medium interaction is about 10 times larger than the classical calculation for the same operating condition, and the pressure for the strong interaction is about 1000 times larger than the classic calculation. It is shown that the adsorbed layer has a very significant effect on the pressure distribution in the bearing, stronger the fluid-bearing surface interaction, more obvious the effect of the adsorbed layer on the hydrodynamic pressure.

Fig. 5 shows the comparison between the pressure distributions with and without the piezo-viscous effect respectively for the strong interaction in the present bearing and for the classical calculation when  $R_z$  is 14nm. The pressure under the piezo-viscous effect is higher than that without the piezo-viscous effect for the strong interaction in the present bearing. The results show that the piezo-viscous effect cannot be ignored for the strong interaction in the present bearing.



Fig. 5 Piezo-viscous effects in the present bearing for the strong interaction and in the classical bearing when  $h_{tot,o} = 10$  nm and  $\theta = 1 \times 10^{-4}$  rad

## 5.2. Carried load of the bearing

Fig. 6 shows the dimensionless carried loads of the bearing with the fluid piezo-viscous effect for different fluid-bearing surface interactions when  $h_{tot,o}$  = =10 nm. With the increase of the surface roughness, the carried load of the bearing is increased significantly. It can be seen that the surface roughness very significantly improves the load-carrying capacity of the present bearing especially for the medium and strong interactions.

## 6. Conclusions

The multiscale calculation was numerically made for the pressure and carried load of the inclined fixed pad thrust slider bearing with ultra low surface separation involving the sinusoidal surface roughness on the stationary surface based on Zhang's multiscale approach and mixed lubrication model [11, 12]. In the present bearing, there are both the boundary lubrication and the sandwich film lubrication.

Based on the obtained results, the conclusions are drawn as follows:

a) The physically adsorbed layer has a very significant effect on the pressure distribution and the carried load of the bearing. The pressure distribution and carried load of the bearing are increased with the increase of the fluid-bearing surface interaction strength.

b) The bearing pressure and load capacity are increased significantly with the increase of the surface roughness. Especially for the strong fluid-bearing surface interaction, the fluid piezo-viscous effect significantly increases the bearing pressures and loads.



Fig. 6 Variation of the dimensionless carried load of the bearing with the surface roughness for different fluid-bearing surface interactions

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W. Zhu, C. Huang, C. Wang, Y. Zhang

# MULTISCALE ANALYSIS AND NUMERICAL SIM-ULATION OF HYDRODYNAMIC INCLINED FIXED PAD THRUST SLIDER BEARING WITH ULTRA LOW SURFACE SEPARATION INVOLVING SURFACE ROUGHNESS

# Summary

In this paper, the hydrodynamic effect in the tilting fixed pad thrust slider bearing with ultra low surface separations is studied by the multiscale analysis considering the nanoscale surface roughness. The flow in the bearing is essentially multiscale incorporating both the adsorbed boundary layer flow and the intermediate continuum fluid flow. The numerical calculation results show that even the surface roughness on the 1nm scale has a strong influence on the generated pressure and carried load of the bearing, and the surface roughness effect strongly depends on the fluid-bearing surface interaction.

**Keywords:** adsorbed layer, hydrodynamic bearing, load, multiscale, surface roughness.

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